

Towards a Conditional Generative Model for Trajectory Modeling in Medical Imaging

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ECSE 556

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Introduction & Motivation



McGill

Generative Models



DALL-E2:

“photograph of an astronaut riding a horse”



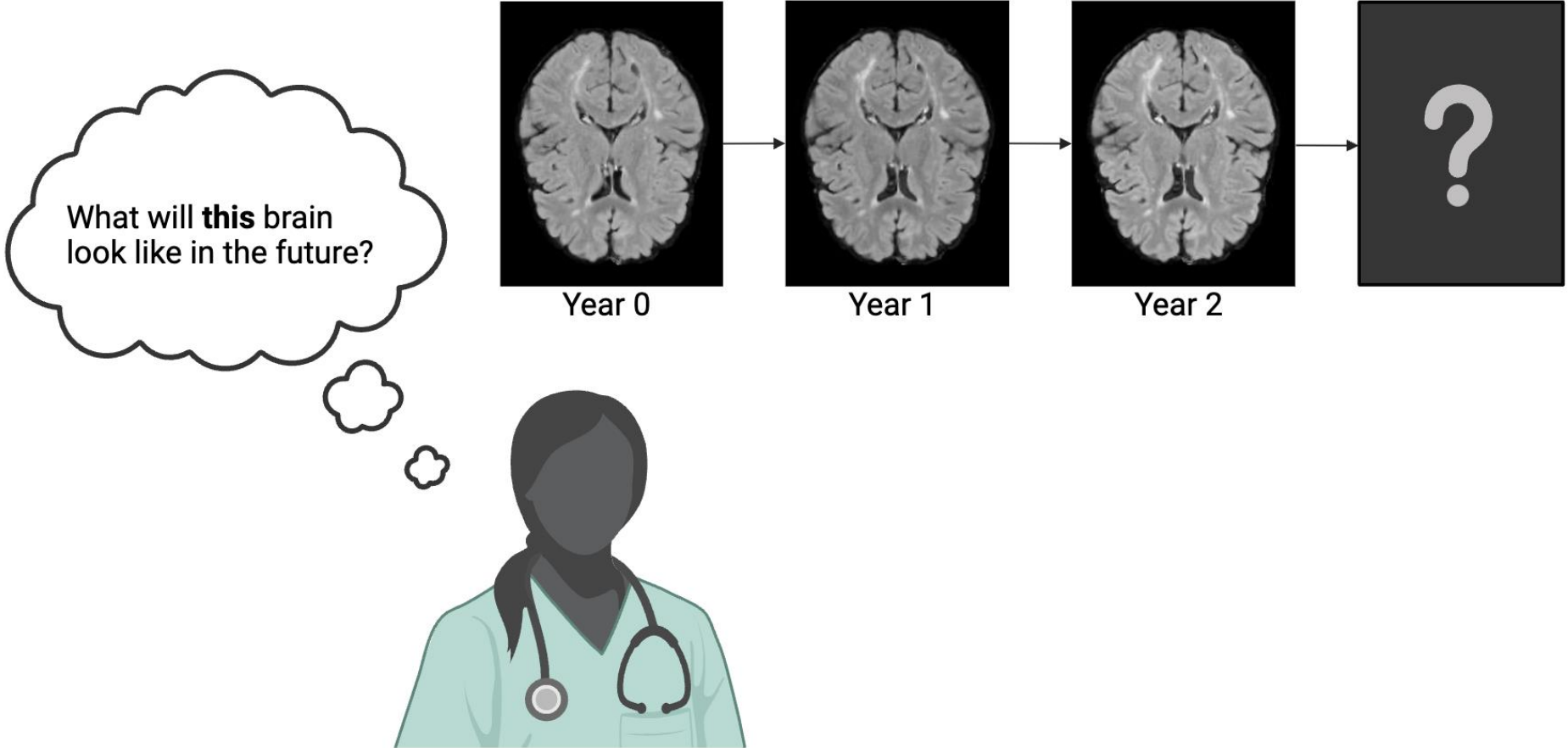
DALL-E2:

“an oil pastel drawing of an annoyed cat in a spaceship”

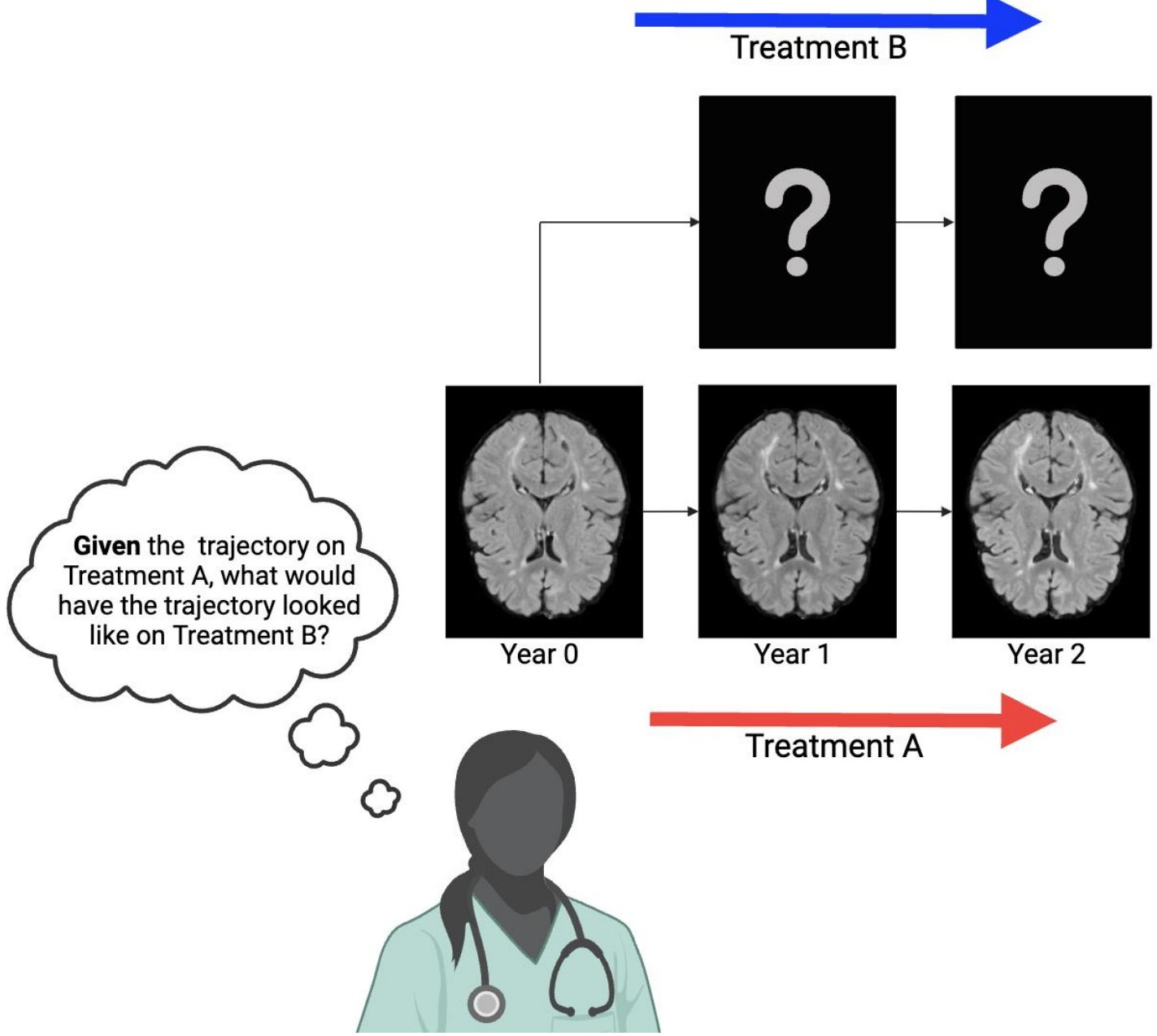


Why is there a need for
generative models in (Multiple
Sclerosis) Medical Imaging?

Disease Progression: Where in the Future?

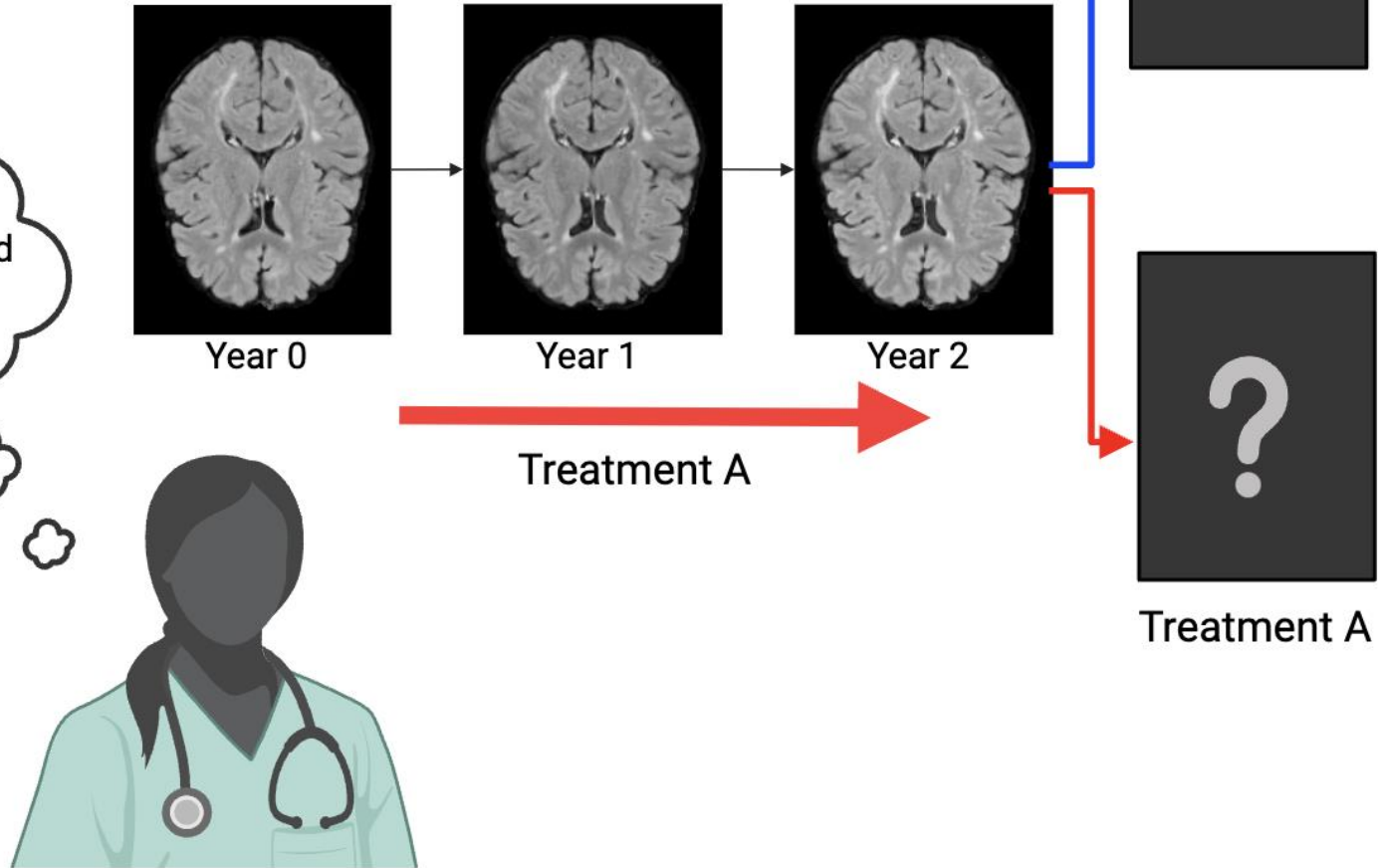


Treatment Effect: Where in the Past?



Personalized Medicine: Where to now?

Given this trajectory
on Treatment A, should
we switch to
Treatment B?



Constraints



McGill

Constraints in (Multiple Sclerosis) Imaging

- We want to generate **patient specific** images
- We want clinically relevant – not random - generation
- We want to distinguish between attributes that are often **highly correlated** (brain morphology and disease progression)

Objectives



McGill

Objectives

1. Generate images such that certain attributes (e.g., number of lesions) are changed
2. Preserve the attribute excluding details (e.g., brain identity, age)
3. Maintain realistic image generation

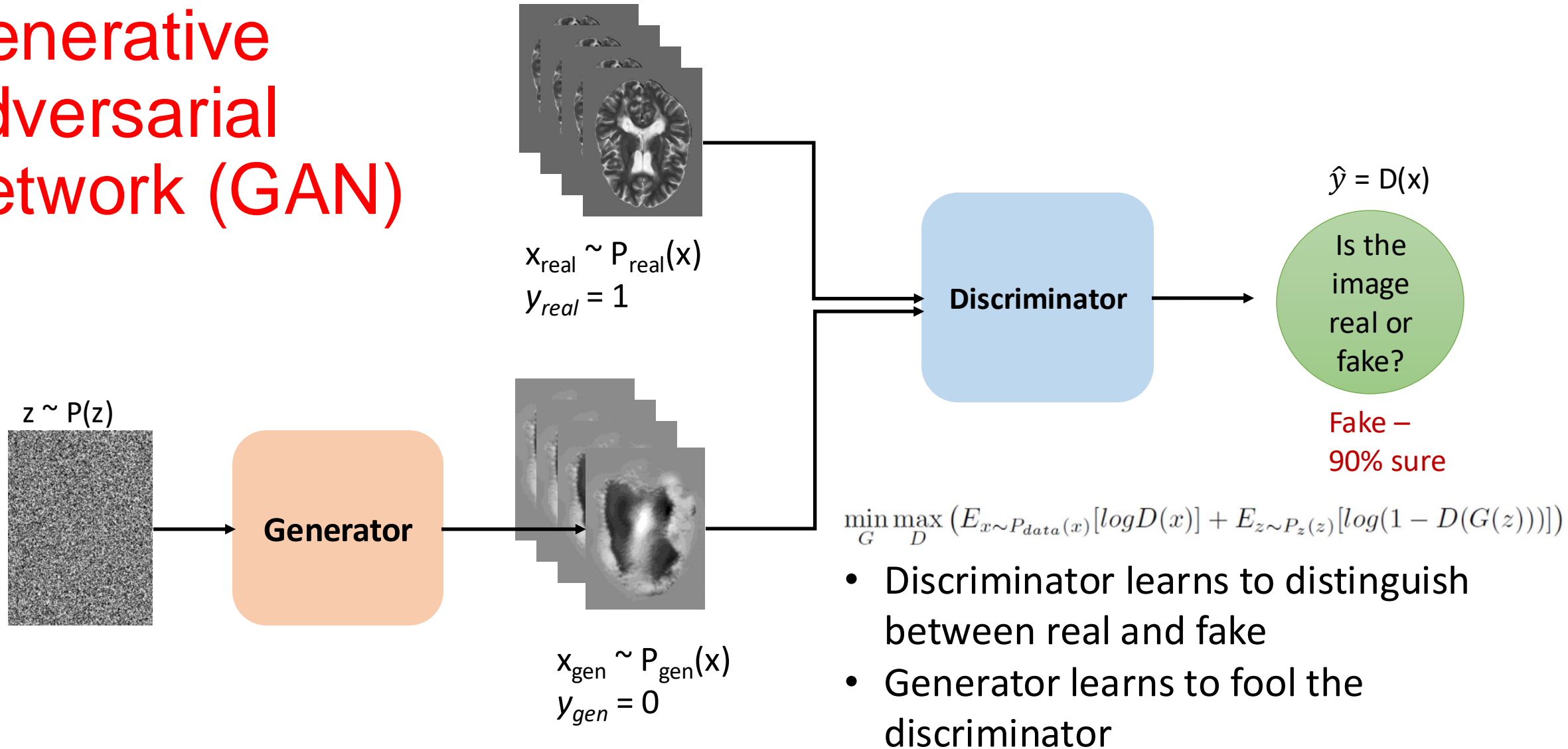
Background



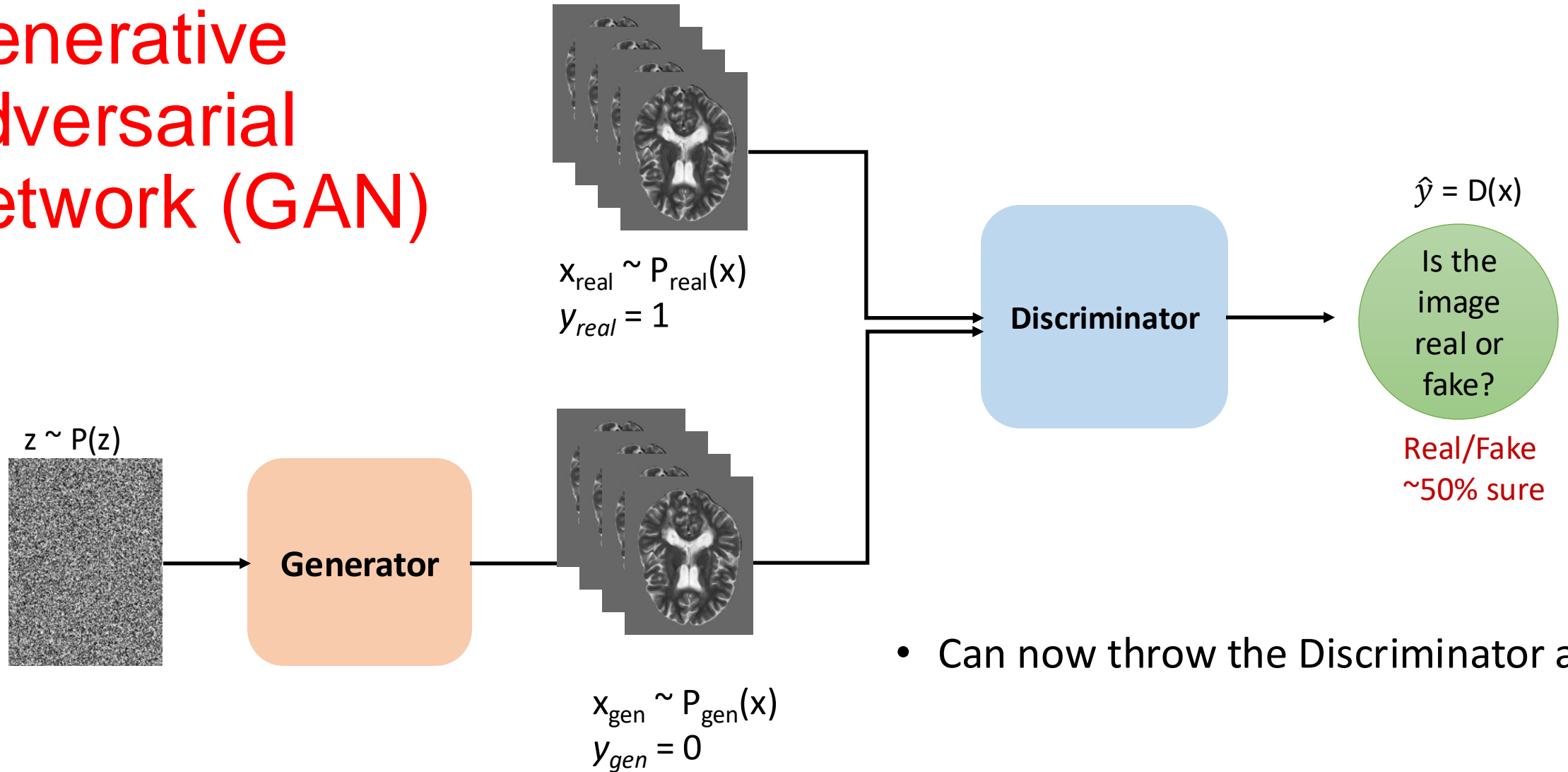
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Generative Adversarial Network (GAN)



Generative Adversarial Network (GAN)



- Can now throw the Discriminator away

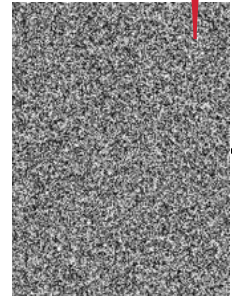
Limitation:

Z-space tied to predefined distribution

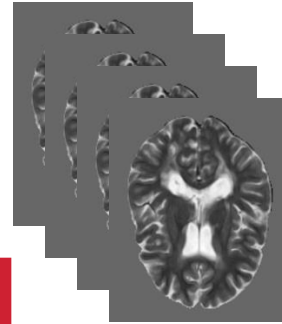
Limitation:

No explicit control of what is being generated!

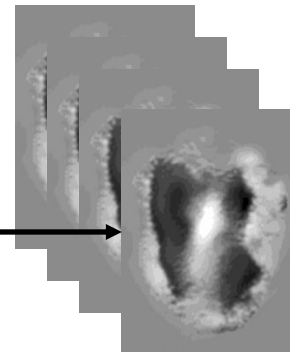
$$z \sim P(z)$$



Generator



$$x_{\text{real}} \sim P_{\text{real}}(x)$$
$$y_{\text{real}} = 1$$



$$x_{\text{gen}} \sim P_{\text{gen}}(x)$$
$$y_{\text{gen}} = 0$$

Discriminator

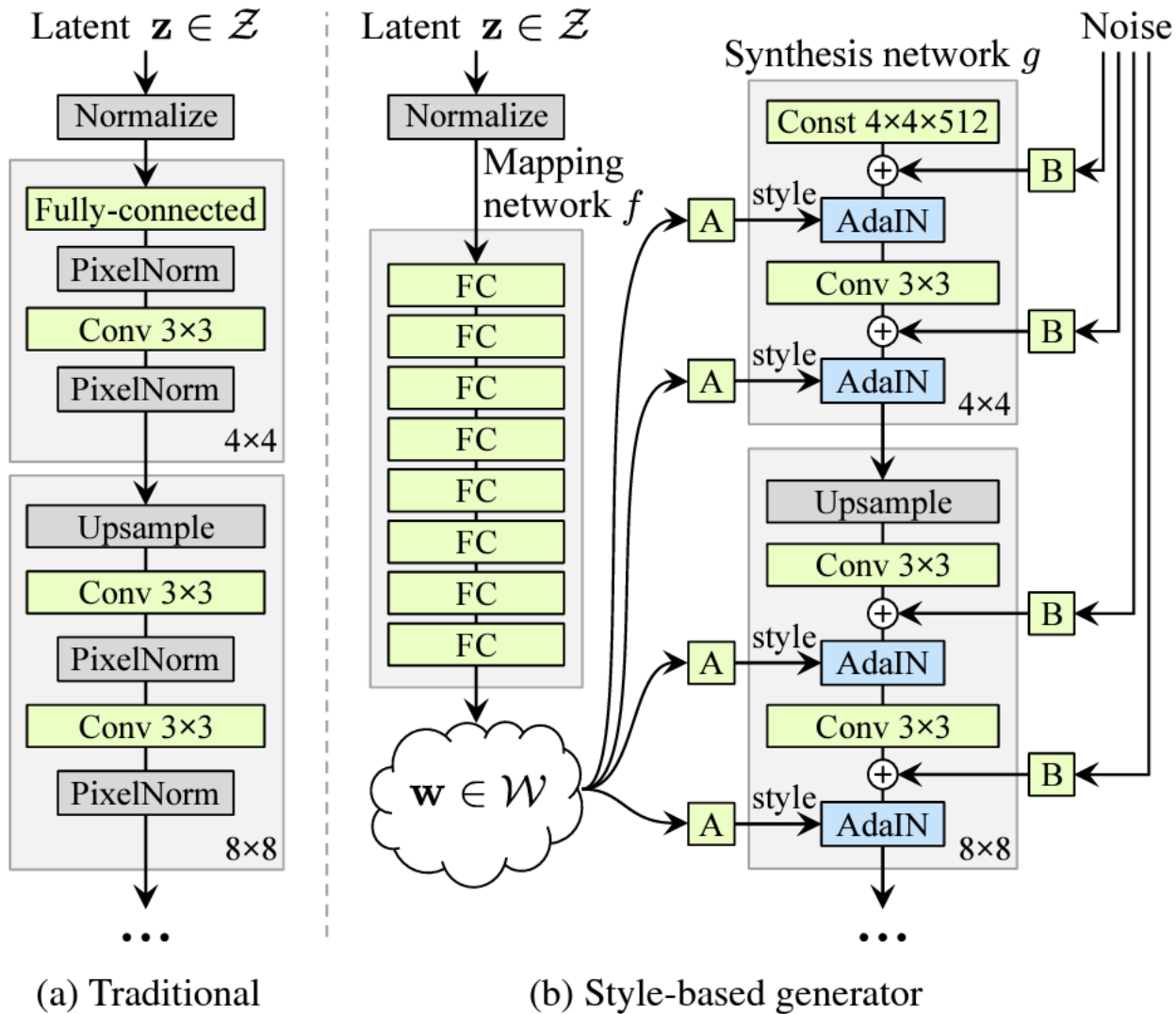
$$\hat{y} = D(x)$$

Is the image real or fake?

$$\min_G \max_D (E_{x \sim P_{\text{data}}(x)}[\log D(x)] + E_{z \sim P_z(z)}[\log(1 - D(G(z)))])$$

- Discriminator learns to distinguish between real and fake
- Generator learns to fool the discriminator

StyleGAN



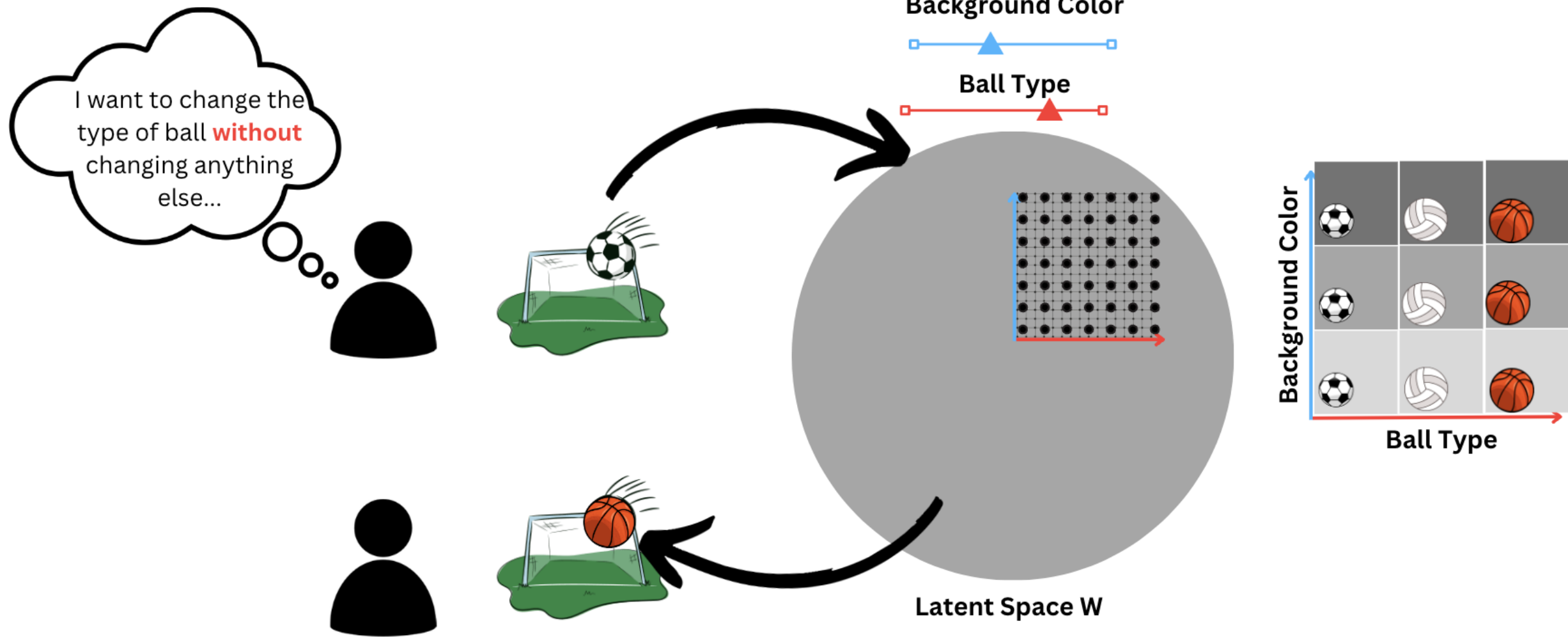
3 major improvements:

- **Mapping network f**
W does not have to support sampling from fixed dist.
- **Adaptive Instance Normalization**
Inject style of y into content of x
$$AdaIN(x, y) = \sigma(y) \left(\frac{x - \mu(x)}{\sigma(x)} \right) + \mu(y)$$
- **Noise**
Induce stochastic variation in the image

Overall idea:

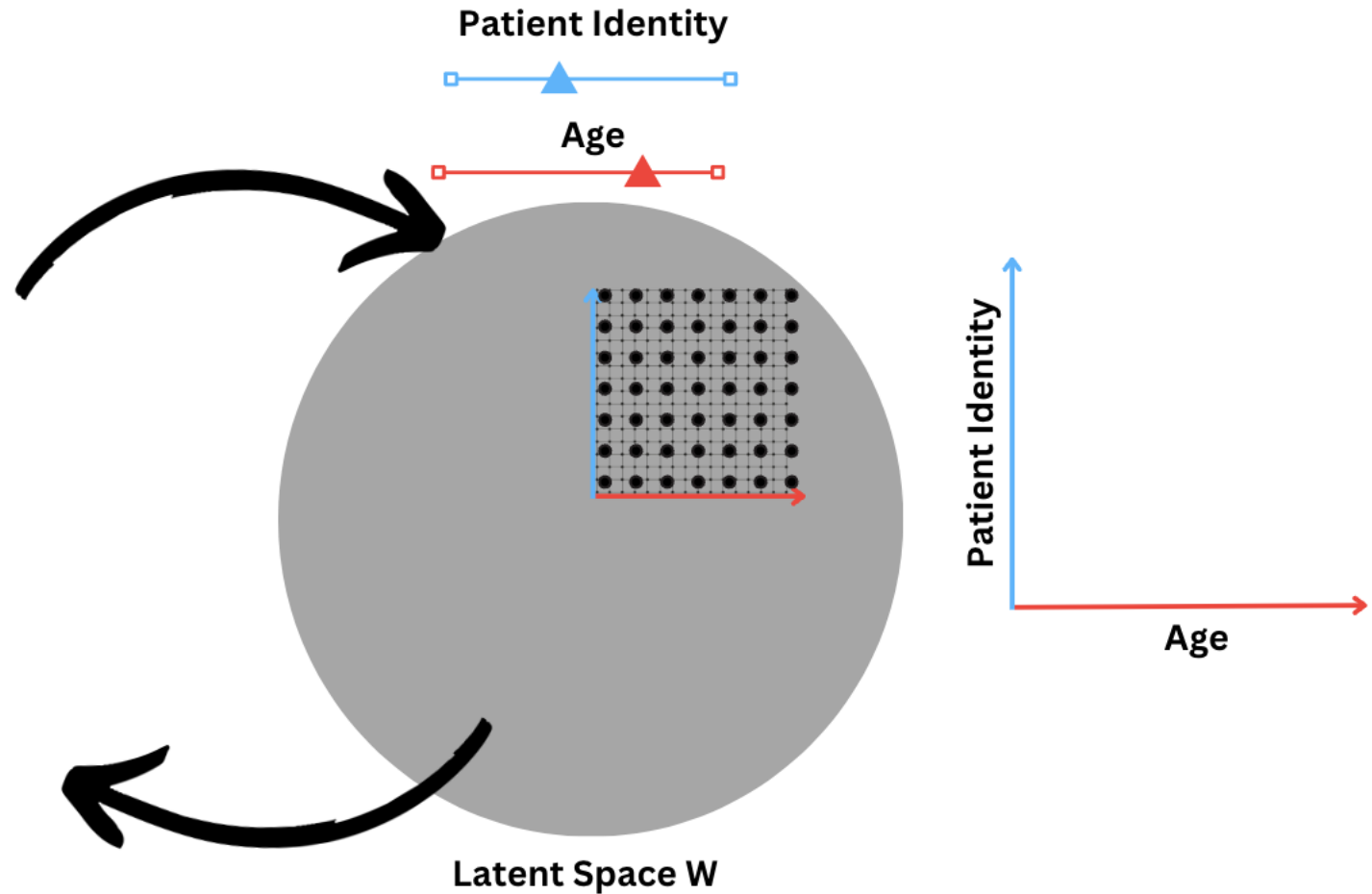
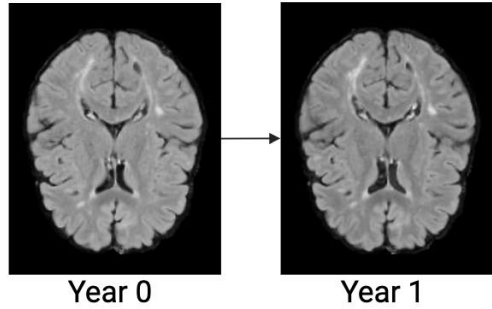
By separating style from content, StyleGAN provides a strong baseline for a **disentangled latent space** where we can theoretically **control** different attributes of an image

Disentanglement for Conditional Generation



Can we apply this to Medical Imaging?

What will **this** brain look like in the future?

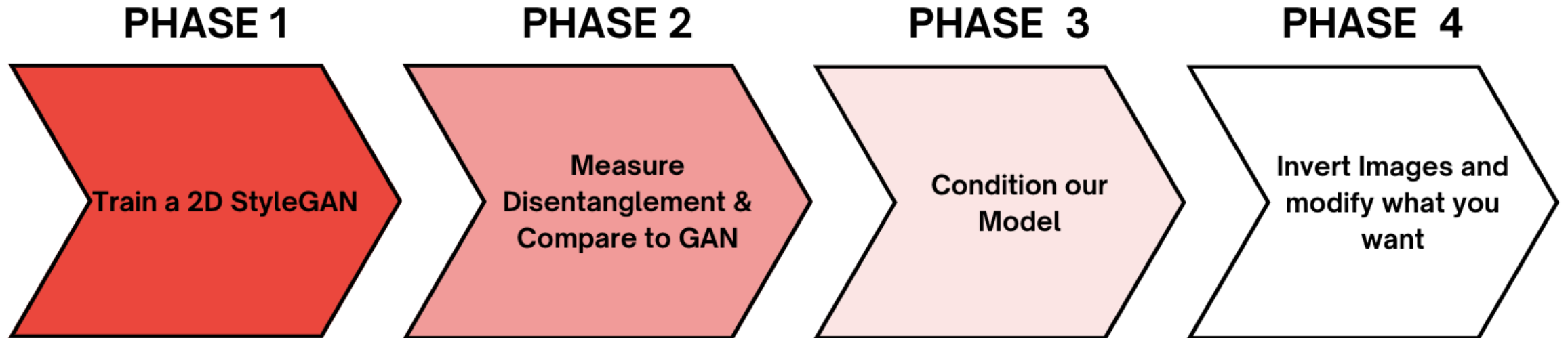


Methodology



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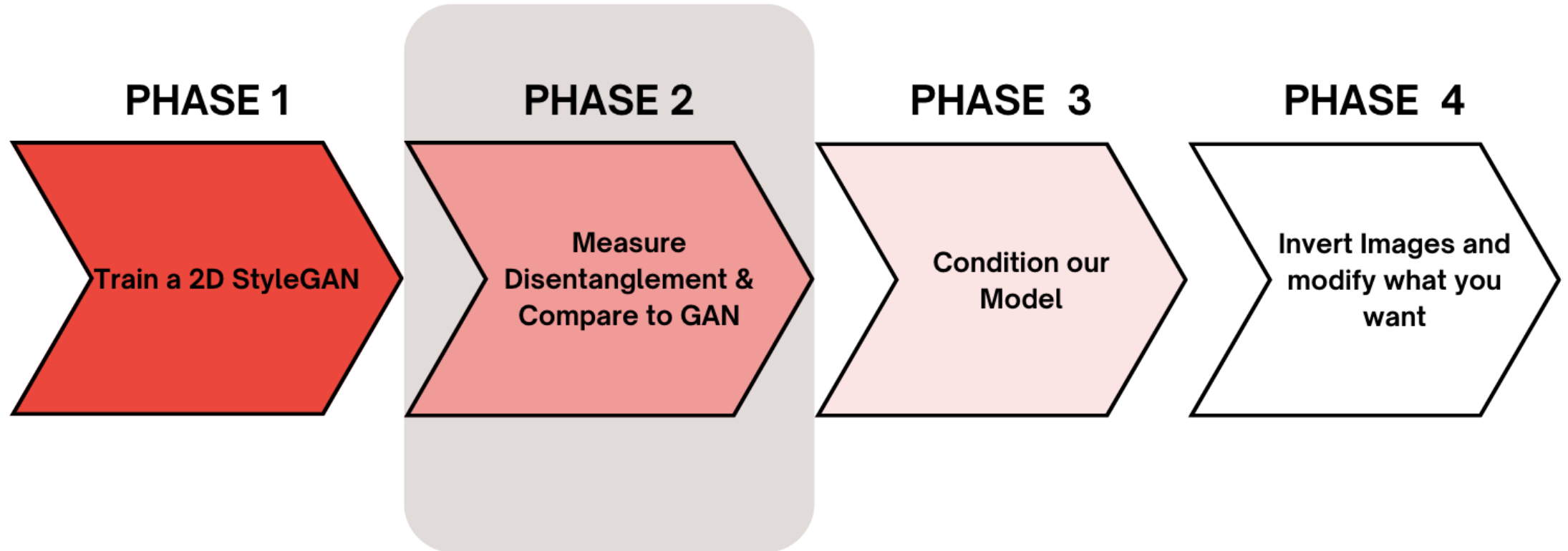
Methodology Pipeline



Dataset & Resources

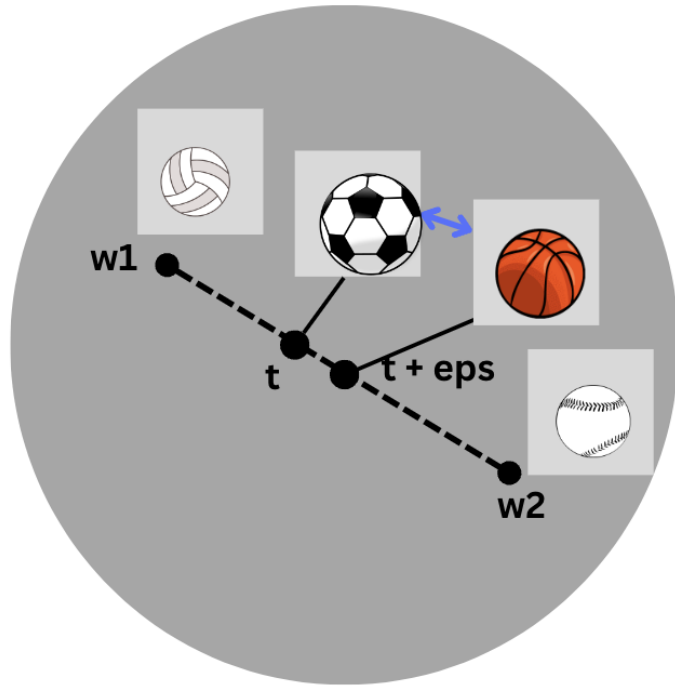
- Multiple Sclerosis with ~5500 patients and access to 16 GB GPUs were provided by the PVG Lab
- Code for a 3D StyleGAN was written at the PVG Lab and thus only needed to be converted to 2D

Methodology Pipeline



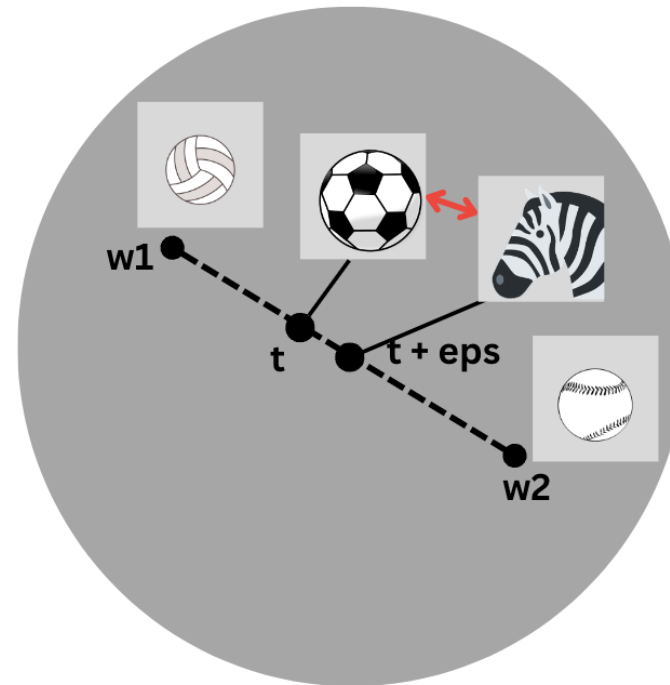
Perceptual Path Length (PPL)

Smaller PPL



Latent Space W

Larger PPL



Latent Space W

Perceptual Path Length:

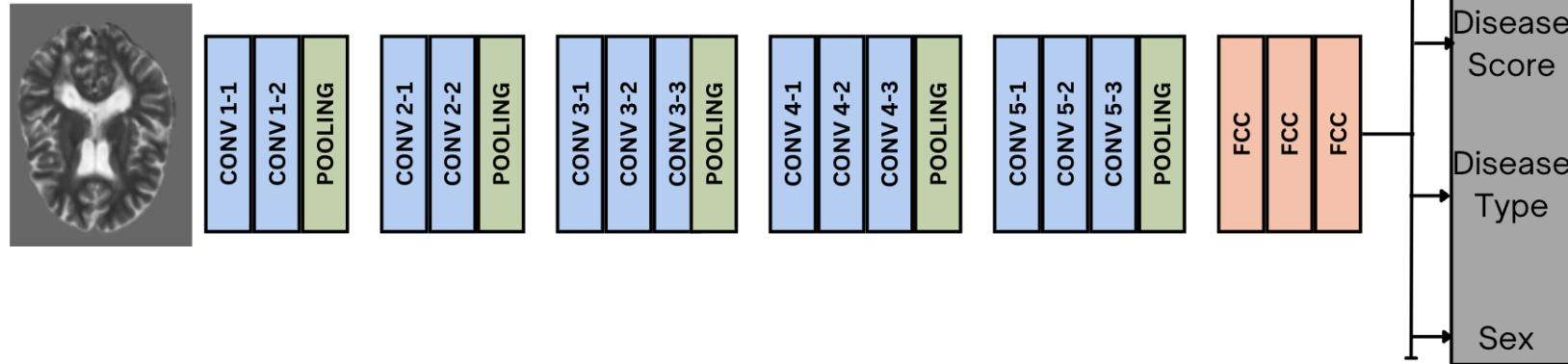
$$l_W = \mathbb{E} \left[\frac{1}{\epsilon^2} d(g(\text{lerp}(f(\mathbf{z}_1), f(\mathbf{z}_2); t)), g(\text{lerp}(f(\mathbf{z}_1), f(\mathbf{z}_2); t + \epsilon))) \right],$$

Idea:

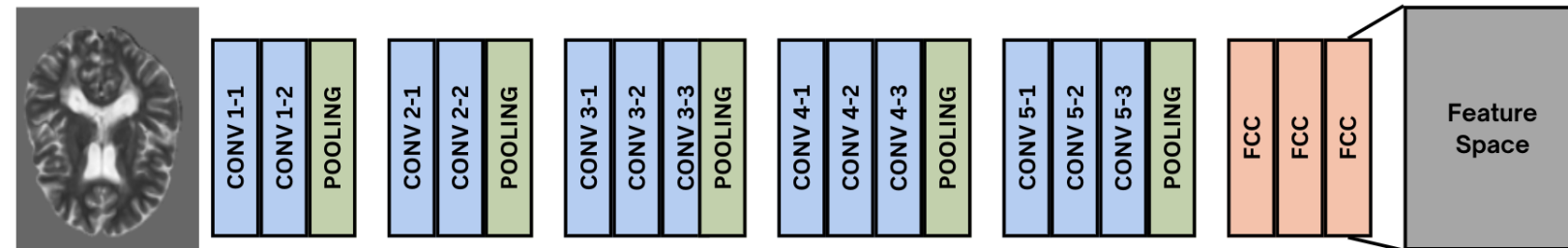
Quantify this distance, d , such that **perceptually** similar images achieve a low PPL score

VGG-16 Model

During Training



At Inference



Perceptual Path Length:

$$l_{\mathcal{W}} = \mathbb{E} \left[\frac{1}{\epsilon^2} d(g(\text{lerp}(f(\mathbf{z}_1), f(\mathbf{z}_2); t)), g(\text{lerp}(f(\mathbf{z}_1), f(\mathbf{z}_2); t + \epsilon))) \right],$$

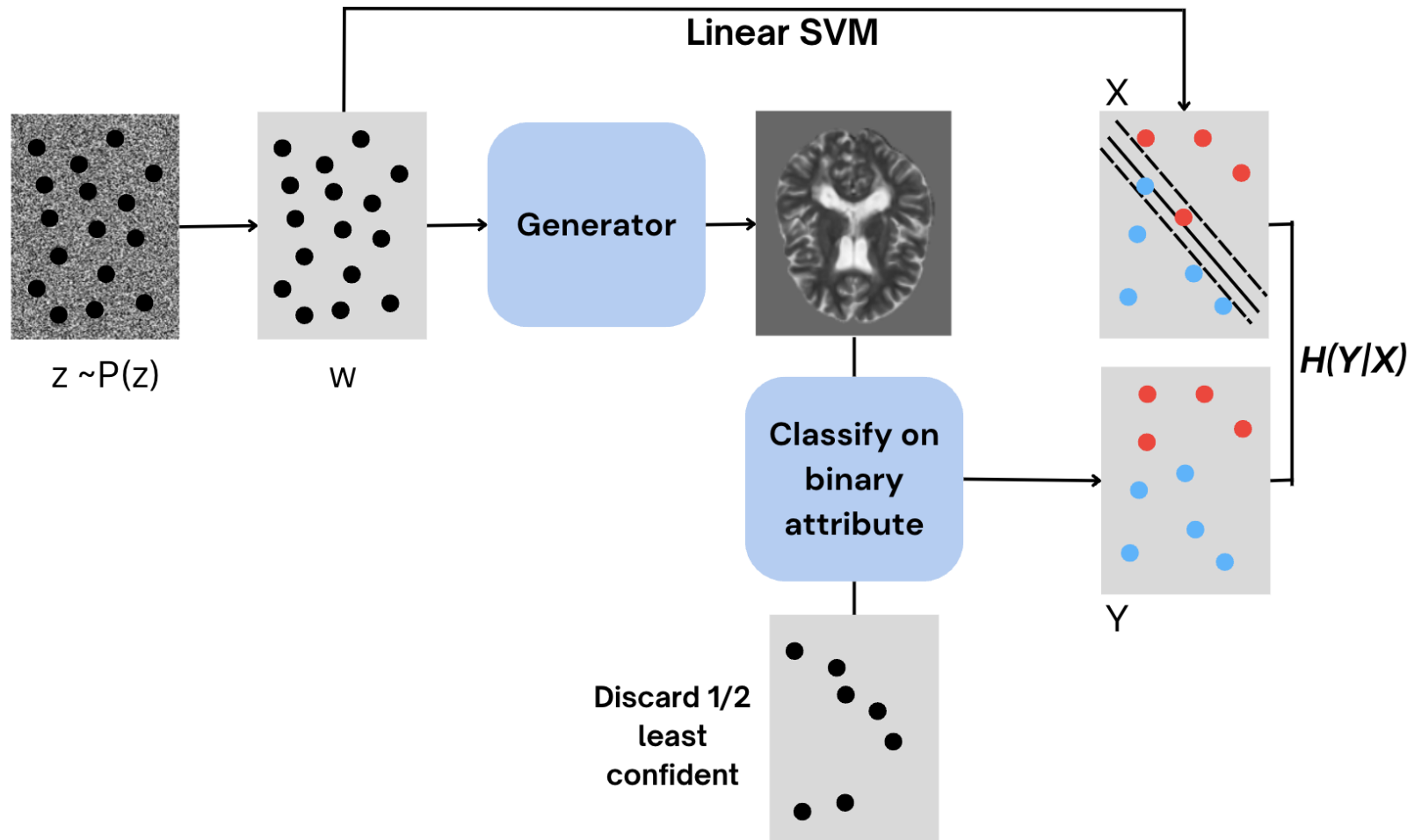
Idea:

Quantify this distance, d , such that **perceptually** similar images achieve a low PPL score

Solution:

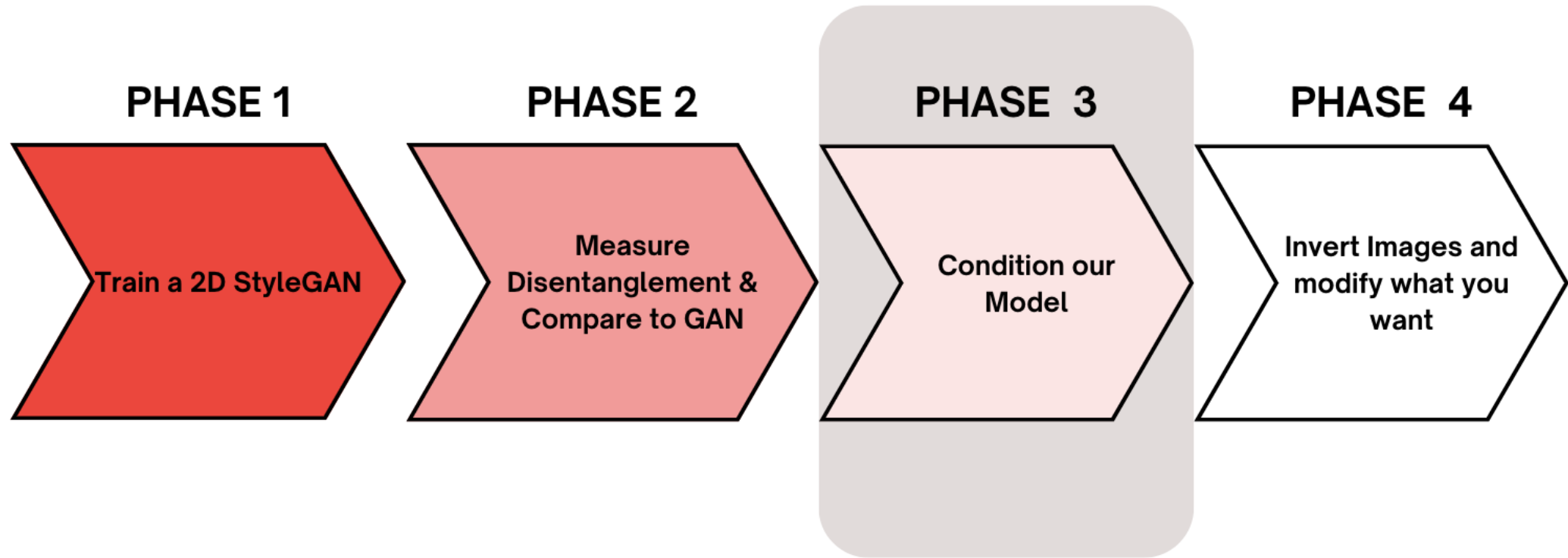
1. Train a VGG-16 model
2. Use its final layer as a feature representation of the image
3. Find the distance between the feature vectors for PPL

Linear Separability

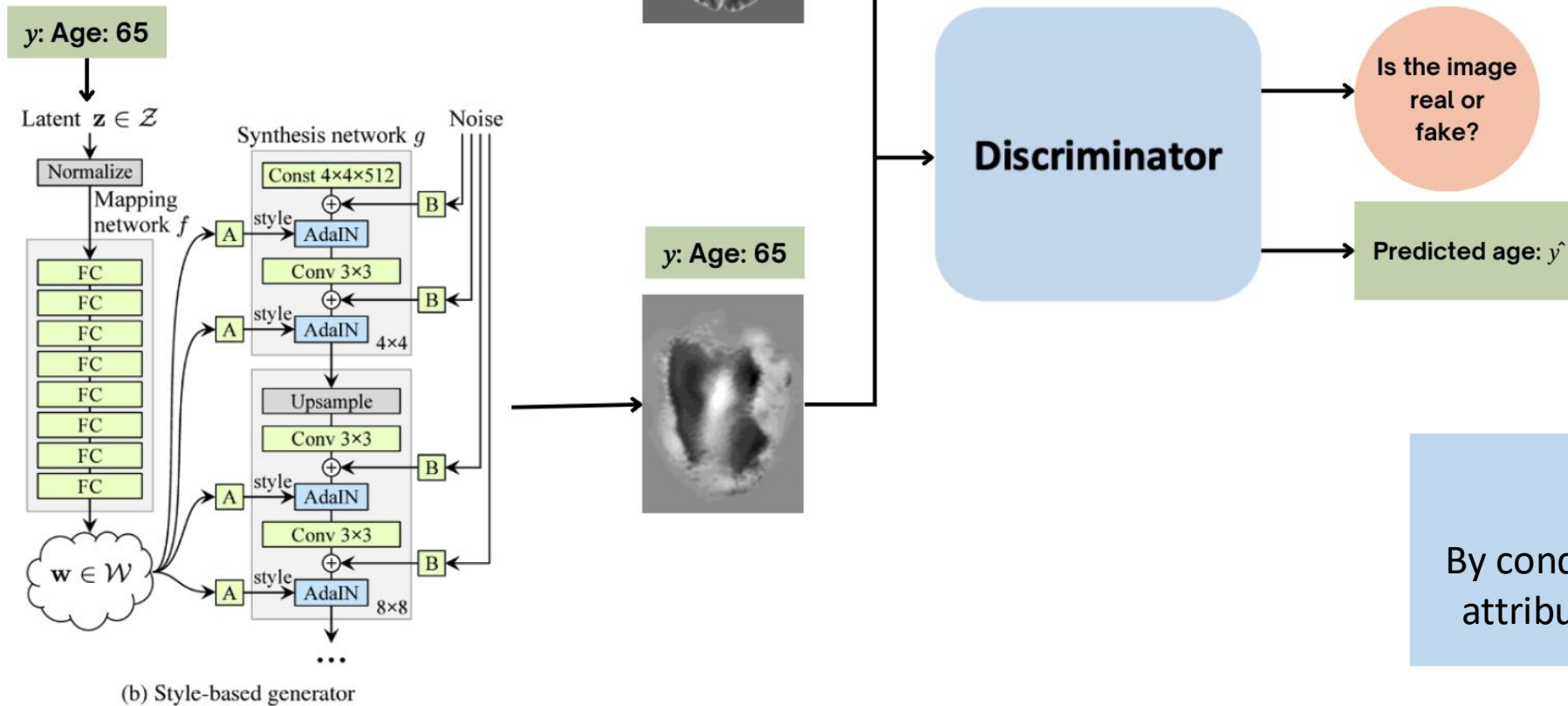


- Idea:**
1. Sample 200,000 points from z space and generate their images
 2. Classify them using a pre-trained classifier based on binary attributes (Y)
 3. Discard the 100,000 least confident images
 4. Fit a linear SVM to categorize latent space points (X)
 5. Compute $H(Y|X)$

Methodology Pipeline



Conditional model



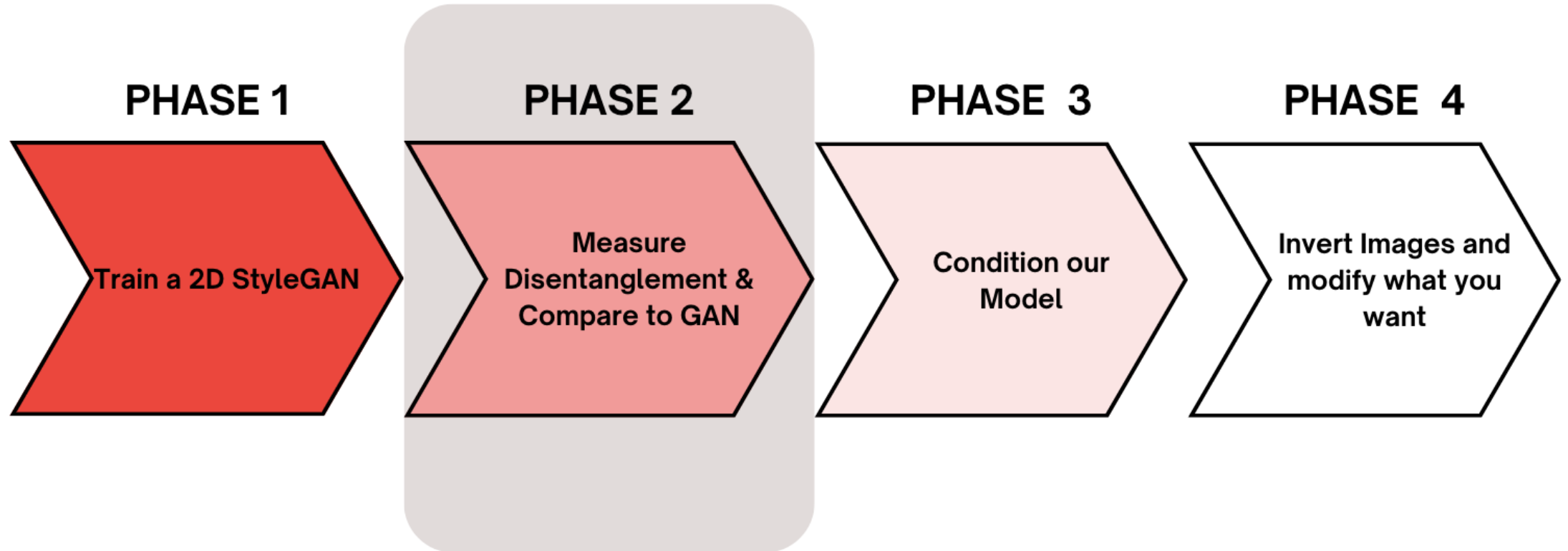
Idea:
By conditioning, we can control for the attributes we want to add or remove

Results

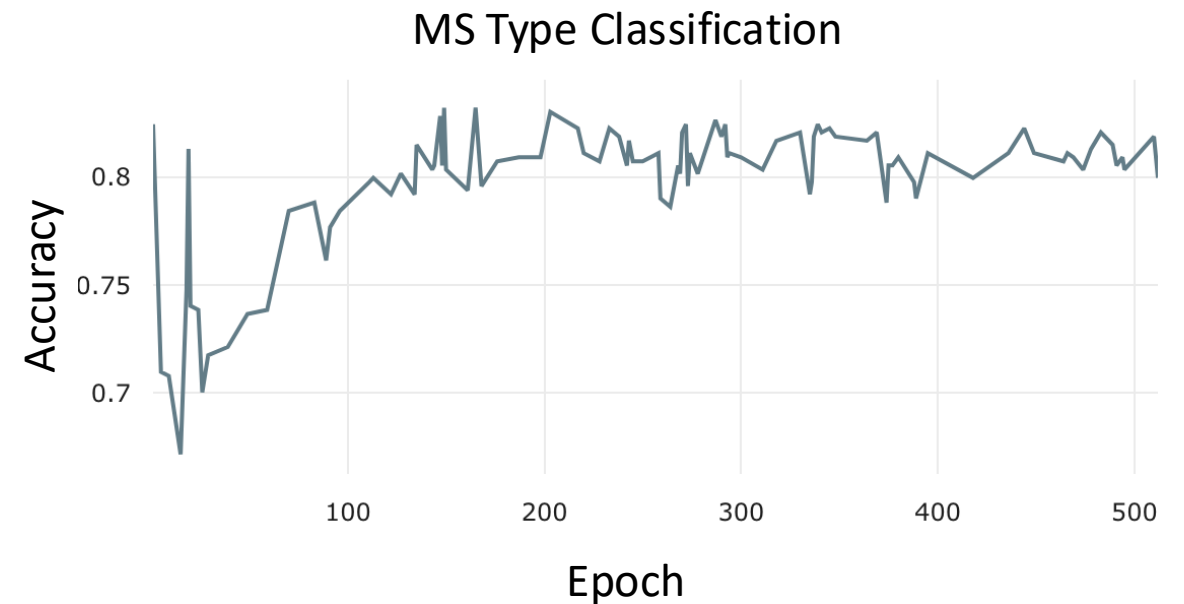
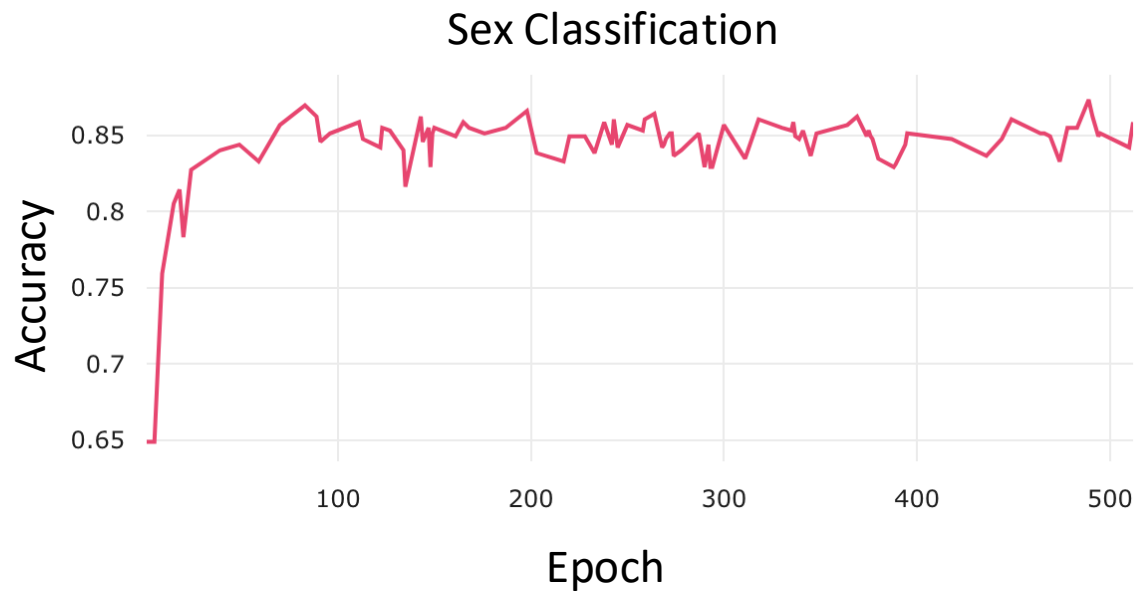


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Methodology Pipeline



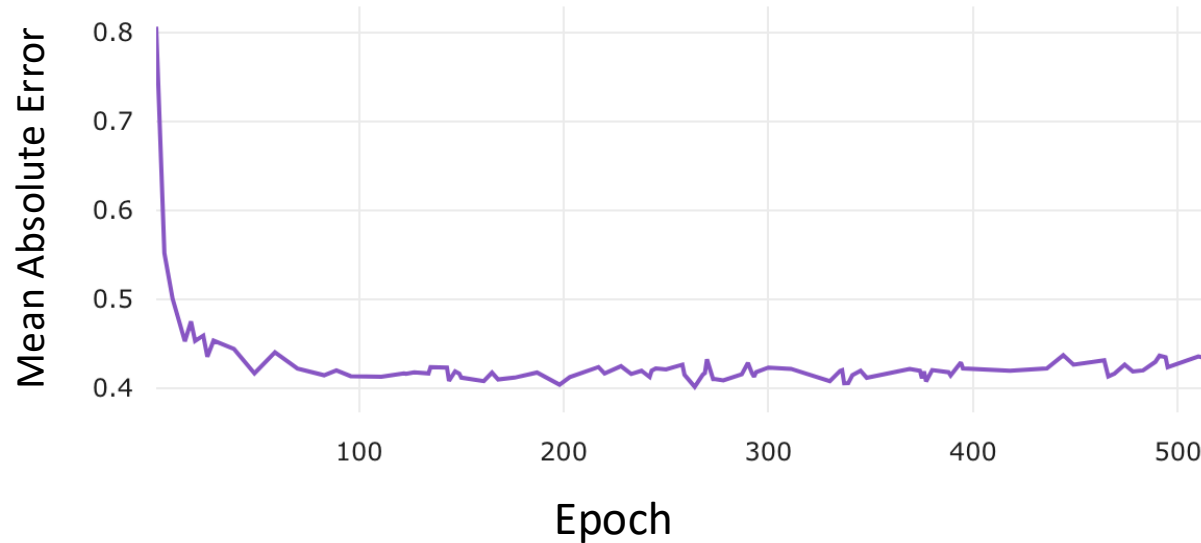
PPL Metric: Training of VGG-16 Model



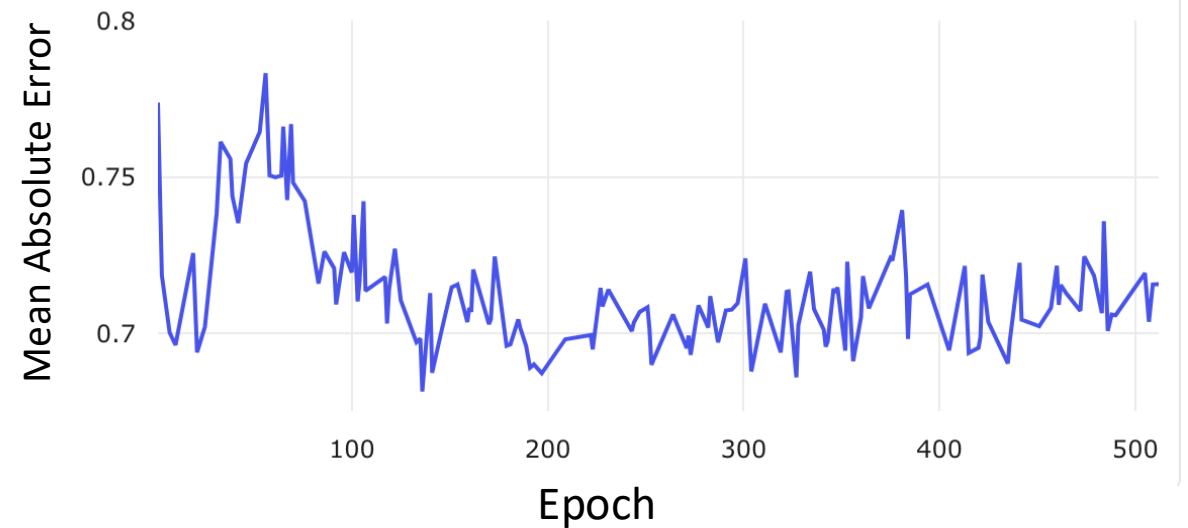
*Reminder: VGG-16 isn't being used to get the most accurate classifier, but rather a feature space corresponding to human perception

PPL Metric: Training of VGG-16 Model

Age Classification

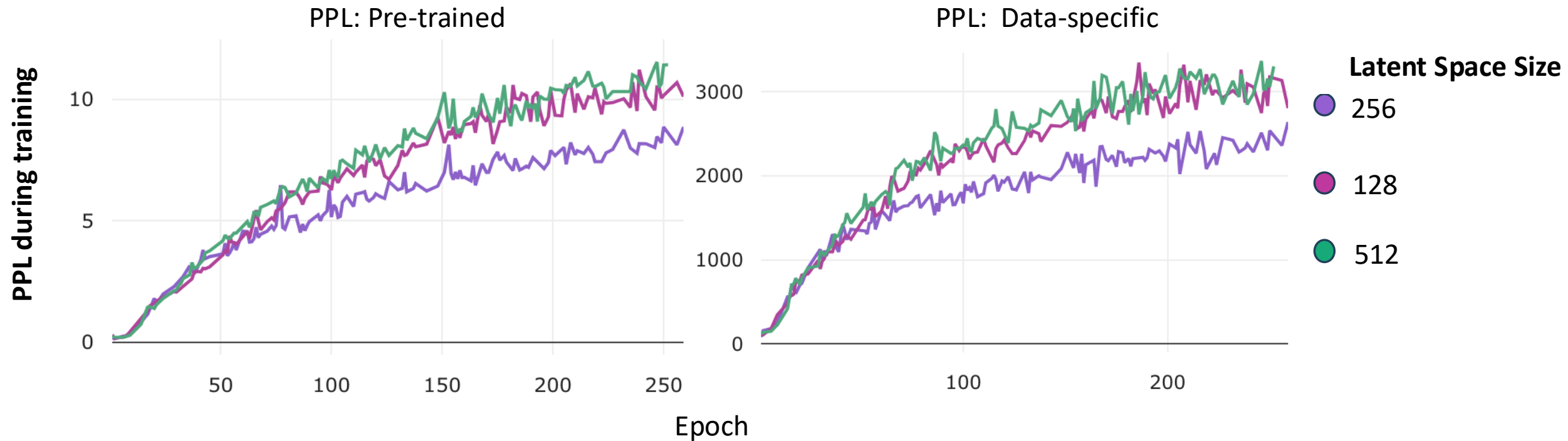


Disease Score Classification



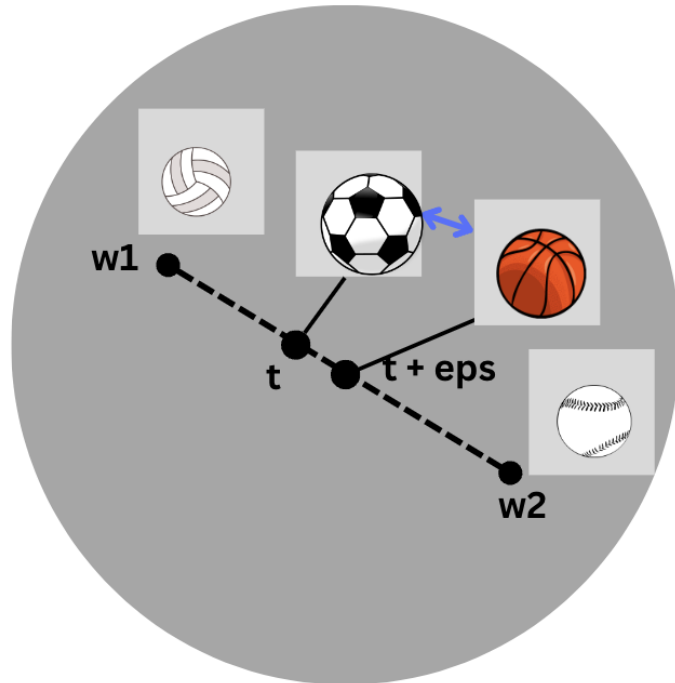
*Reminder: VGG-16 isn't being used to get the most accurate classifier, but rather a feature space corresponding to human perception

PPL Metric: Comparison of our model with pre-trained VGG-16



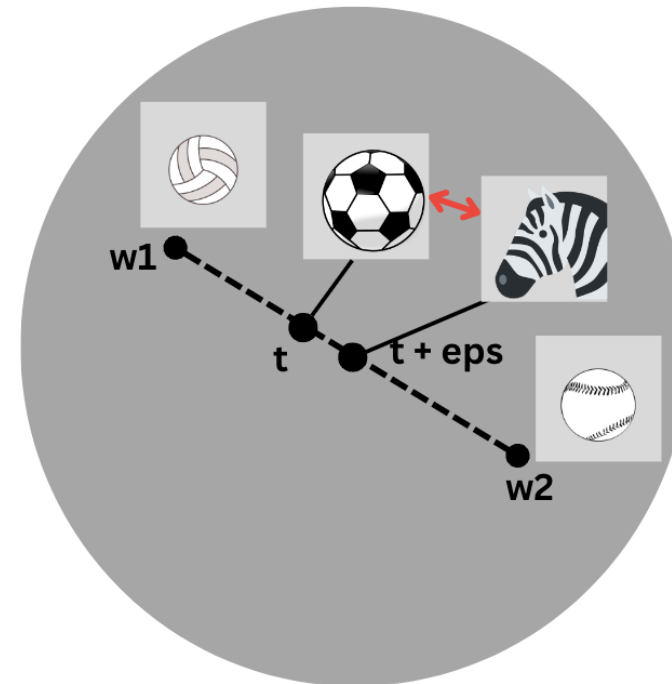
StyleGAN Interpolations

Smaller PPL



Latent Space W

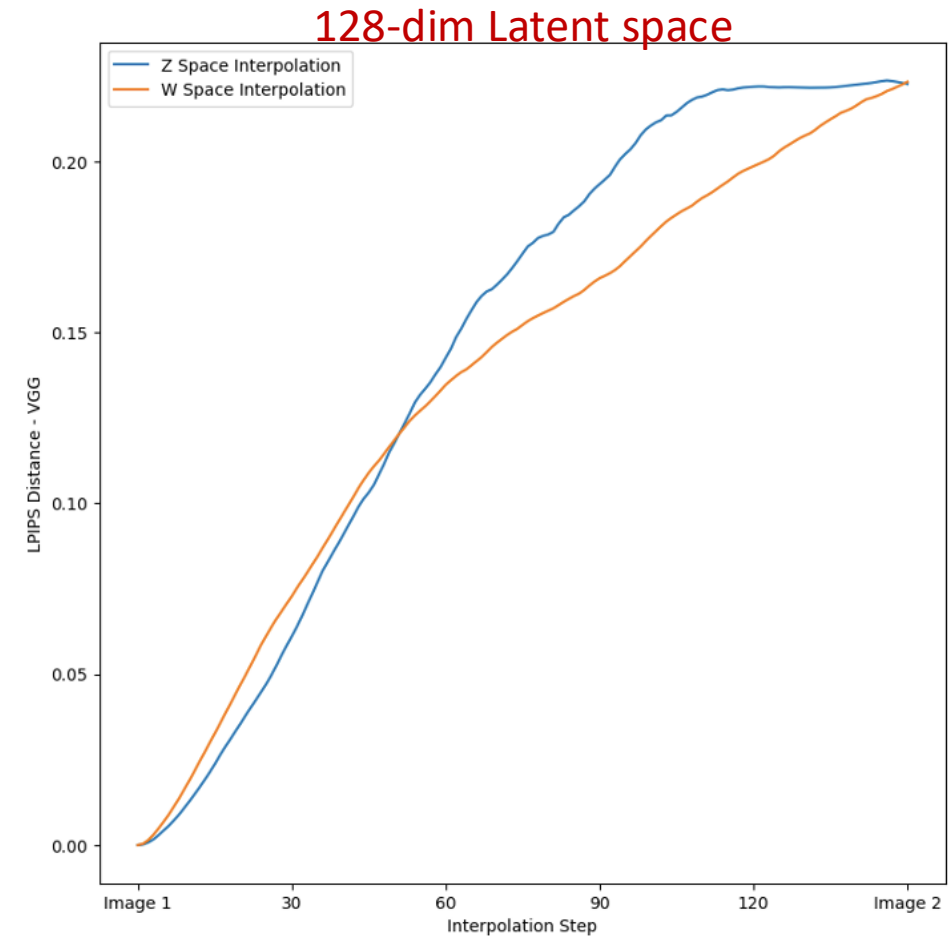
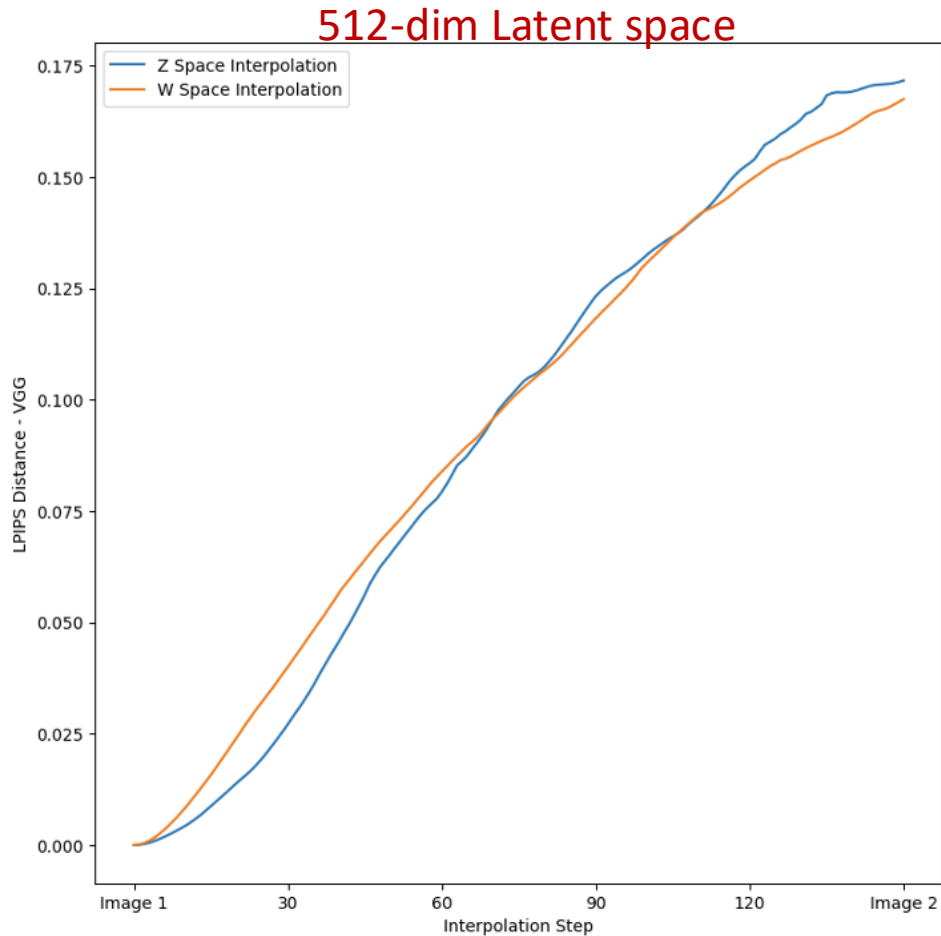
Larger PPL



Latent Space Z

- Intuitively, we expect that if we **linearly** interpolate in Z-space (Gaussian!), changes in the image space will **not** be smooth
- If overparameterized (too big latent space), model can learn smooth transitions
- Ideally, smaller latent space would mean more precise conditioning

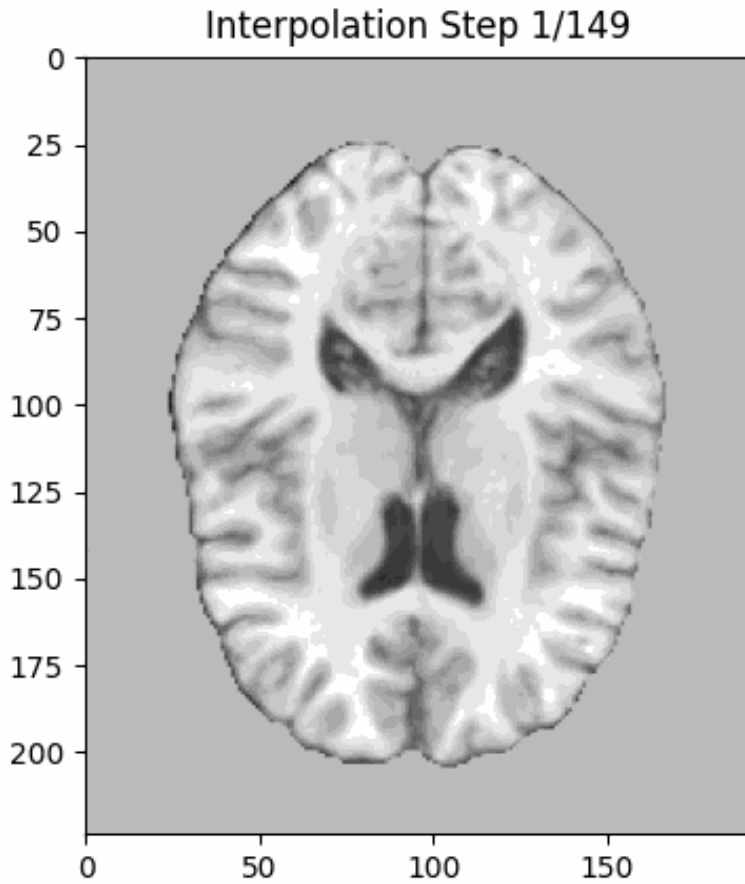
StyleGAN Interpolations



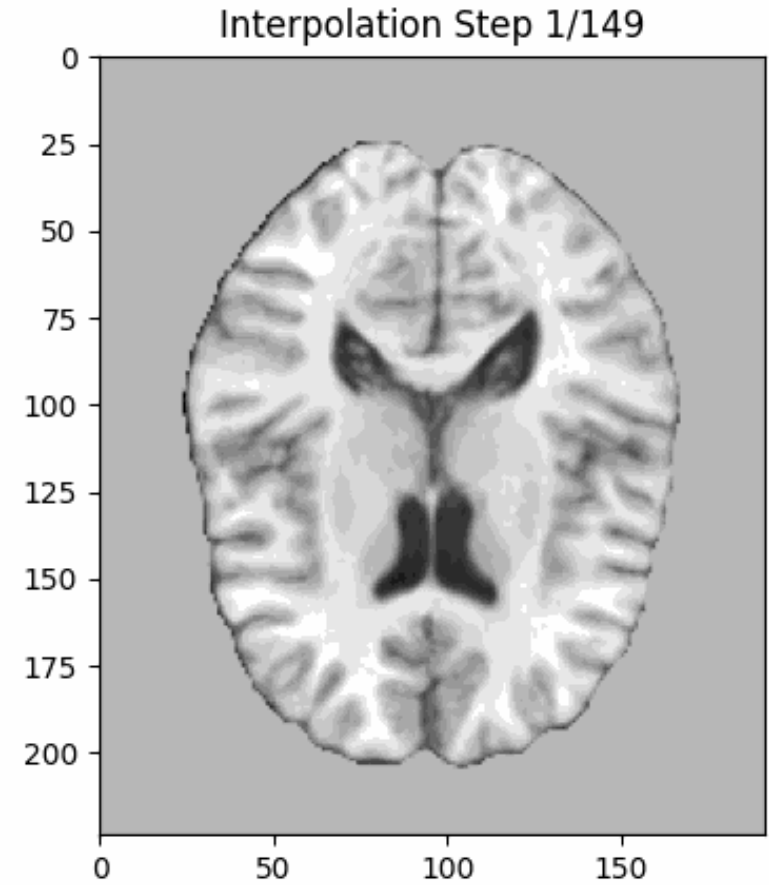
- Intuitively, we expect that if we **linearly** interpolate in Z-space (Gaussian!), changes in the image space will **not** be smooth
- If overparameterized, model can learn smooth transitions

StyleGAN Interpolations: 512-dim latent

W SPACE

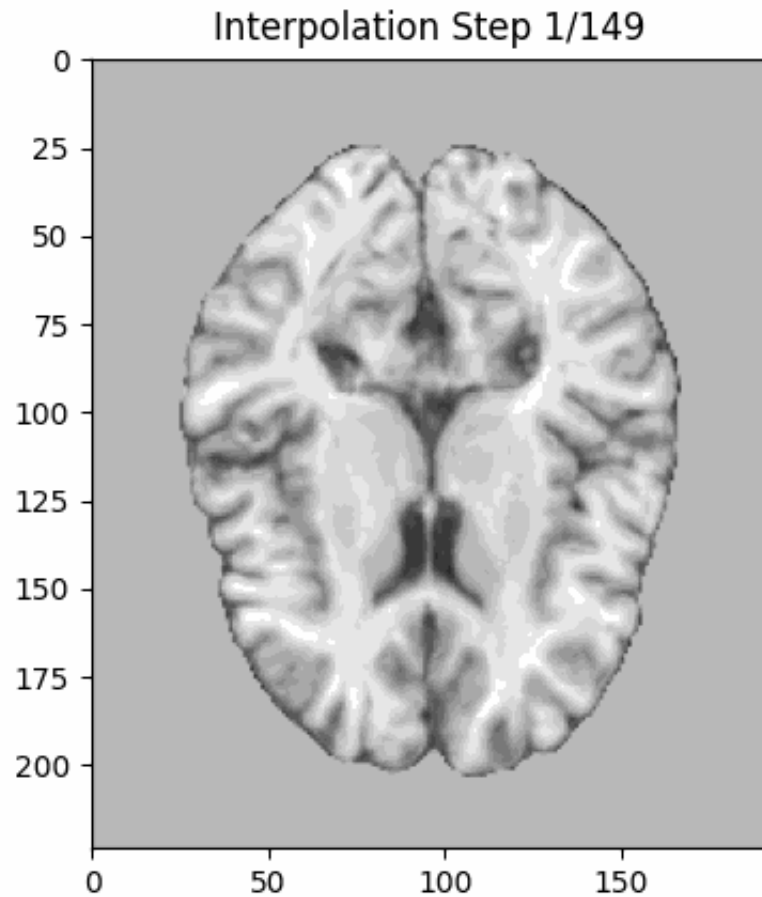


Z SPACE

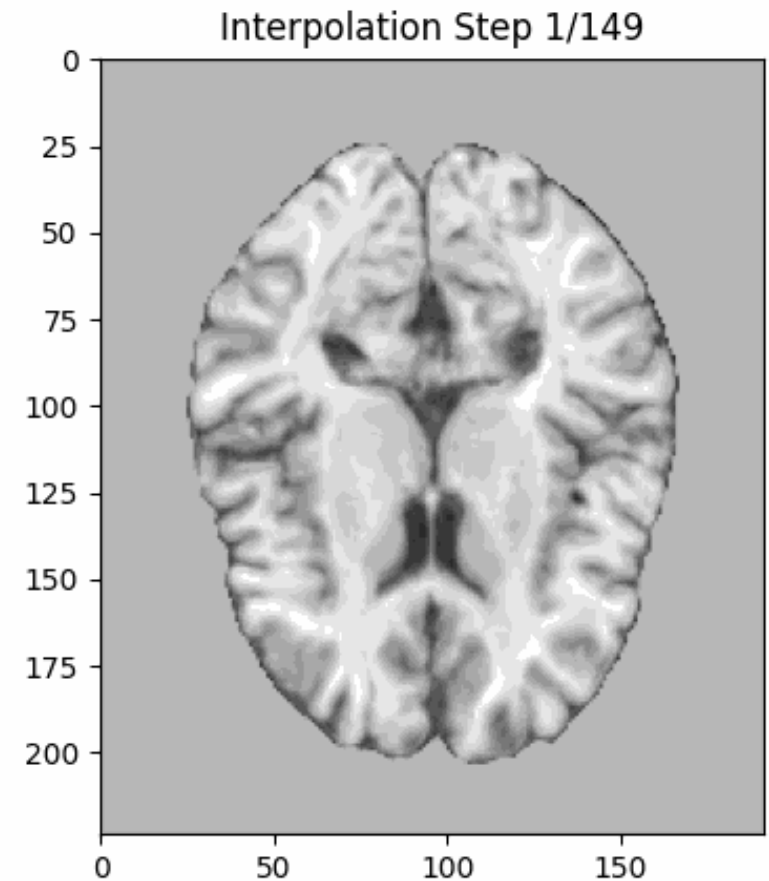


StyleGAN Interpolations: 128 dim latent

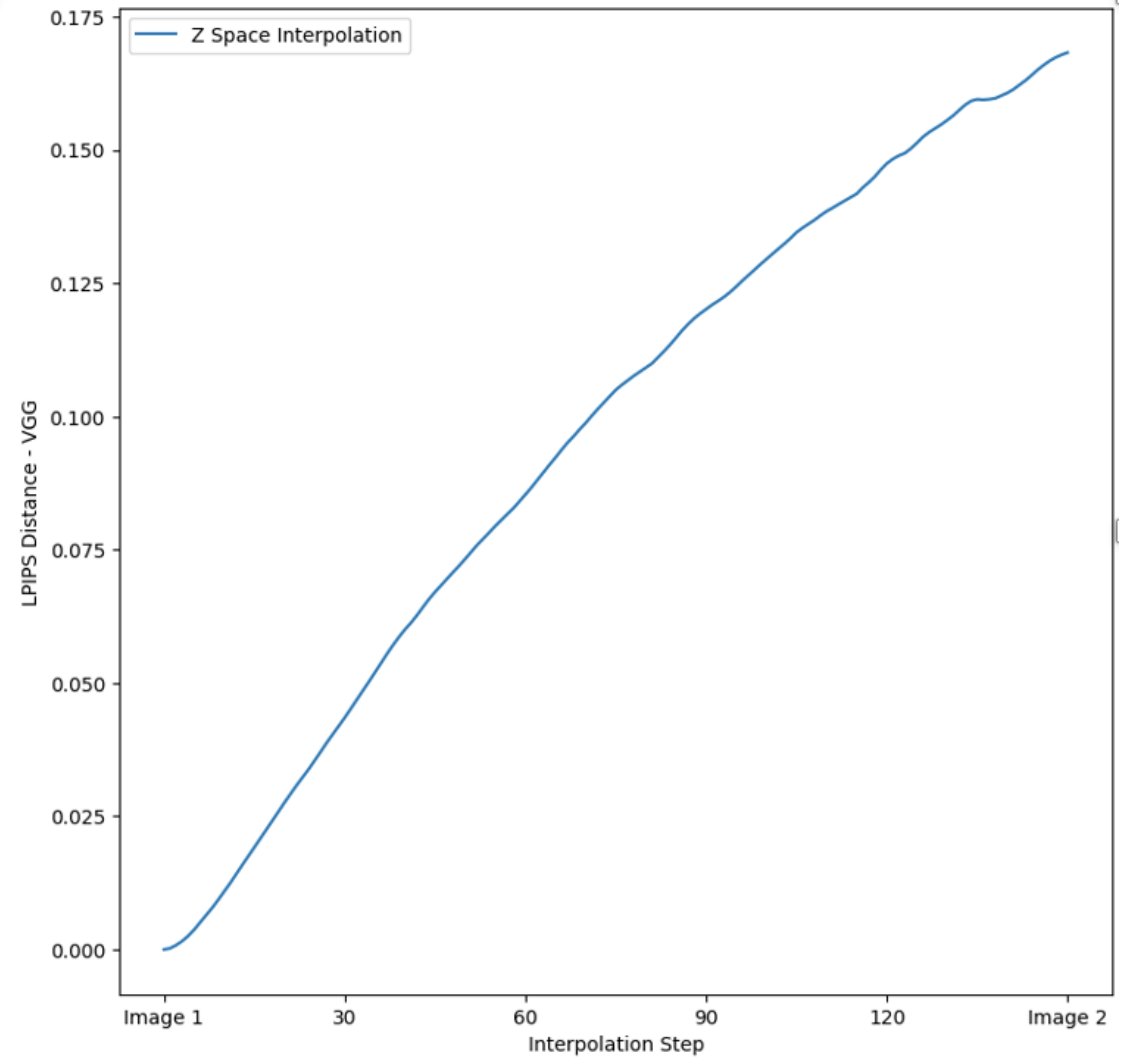
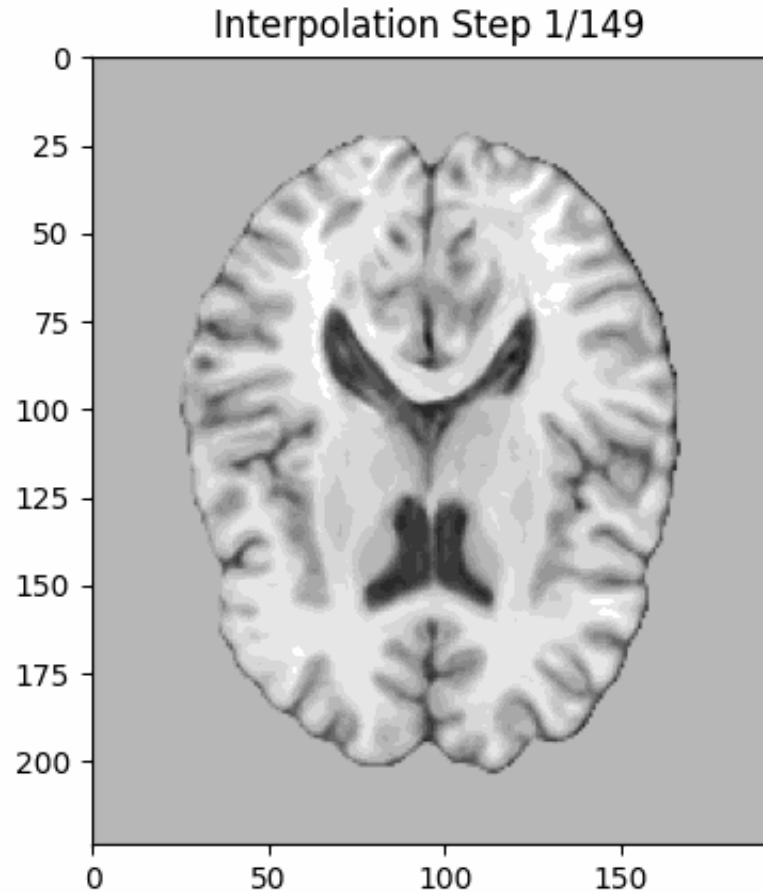
W SPACE



Z SPACE



GAN Interpolations: 256-dim latent



Future Work



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Future Work

- Try smaller latent space sizes...currently overparameterized
- Add linear separability metric (amongst others)
- Evaluate metrics for StyleGAN vs GAN architecture
- Add conditioning and see if disentanglement improves
- Perform inversions...